

1 **Biodiversity conservation in a dynamic world may lead to inefficiencies due to lock-in**
2 **effects and path dependence**

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5
6 **Abstract**

7 Although biodiversity is still diminishing at an alarming rate, in some areas its conservation is
8 expanding. The exact path of this expansion, however, is uncertain. This can lead to problems
9 of path-dependence and lock-in effects. Path dependence describes situations where history
10 strongly influences present decisions and lock-in effects refer to situations where an earlier
11 decision provides strong incentives to follow a particular path, even if more efficient
12 alternatives are available later on. Both concepts have been studied by economists and social
13 scientists in various applications. However, to our knowledge these concepts have not been
14 applied to the analysis of biodiversity conservation policies and strategies in a modelling
15 framework. Here, we develop a conceptual ecological-economic model to investigate which
16 ecological and economic parameters favour the appearance of efficiency losses in biodiversity
17 conservation due to path dependence and lock-in effects in a dynamic two-period two-region
18 model. Generally we find that efficiency losses occur if there are signals that guide the first-
19 period budget into a region that later turns out to be suboptimal if both time periods had been
20 considered right from the beginning. This is, for example, the case if level and slope of
21 marginal costs are small in the region with the less convex ecological benefit function, so that
22 the first-period budget is misguided into the less costly region, ignoring that for larger budgets
23 the ecological benefit is lower than in the other region. To illustrate the conservation
24 relevance of our findings, we present potential efficiency losses through path dependence in
25 the hypothetical case of applying offsets to conserving the endangered *Maculinea teleius*
26 butterfly near the city of Landau in Germany.

27
28 **Key words:** dynamic optimisation, ecological-economic model, ecological benefit, economic
29 cost, efficiency, resource allocation.

30 **Introduction**

31 Global biodiversity is declining at an alarming rate (Butchart et al. 2010). Despite this general
32 negative trend, biodiversity conservation is expanding in some areas. Examples include the
33 enlargement of reserve sites (Morales-Hidalgo et al. 2015), the generation of new habitats
34 through financial means from offsets (Wende et al. 2018), the implementation of conservation
35 easements (Rissmann et al. 2013), and land purchase by conservation agencies and NGOs
36 (Schöttker and Wätzold 2018). This expansion, however, is typically slow and the exact path
37 of expansion is unknown as the future political situation regarding biodiversity conservation
38 (Haila and Henle 2014) and the availability of future conservation budgets (Drechsler and
39 Wätzold 2007) are full of uncertainties. This means that decision makers have to make
40 conservation decisions today without knowing to what extent conservation expansion is
41 possible in the future.

42 In their analyses of decisions and their consequences in a dynamic and uncertain world,
43 economists and social scientists have identified path dependence and lock-in effects as
44 important factors that affect the long-term consequences of present decisions and may lead to
45 inefficiencies (David 1985, North 1991). The concept of path dependence typically is used to
46 describe situations where history, i.e. previous conditions, strongly influences present
47 decisions (Liebowitz and Margolis 1995). The term lock-in has been used to explain that an
48 earlier decision provides strong incentives to follow a particular path – to be locked-in in that
49 path - even if more efficient alternatives are available later on (David 1985). Applications of
50 the concepts of path dependence and lock-in effects are found in the fields of technology
51 development (Ruttan 1997), organisational analysis (Sydow et al. 2009), and institutional
52 change (North 1991), among others.

53 There are also some studies that use these concepts in environmentally related research.
54 Barnett et al. (2015) investigate how the path-dependent nature of the institutions limit

55 today's climate change adaptation in Australia. Unruh and Carrillo-Hermosilla (2006) argue
56 that due to industrial lock-in effects developing countries are unlikely to leapfrog carbon
57 intensive energy production, and regarding agricultural land use, Sutherland et al. (2012) use
58 path dependence to explain farmers' resistance to move towards environmentally beneficial
59 land use. The closest analysis to biodiversity conservation that we found is the application of
60 the concept of path dependence to explain the emergence of payments for ecosystem services
61 (Bidaud et al. 2013). However, to our knowledge, there is no further research that applies the
62 concept of path dependence and lock-in effects in a systematic manner to biodiversity
63 conservation policies and strategies.

64 This is somewhat surprising as there is quite a lot of literature about biodiversity conservation
65 in a dynamic and uncertain world (Costello and Polasky 2004, Meir et al. 2004, Pressey et al.
66 2007). For example, Johst et al. (2011) and Van Teeffelen et al. (2012) discuss the impact of
67 habitat network dynamics on species conservation. Adopting a more historical perspective
68 Dallimer et al. (2009) address land use change, habitat change, and how stakeholders perceive
69 it in the Peak District in England. Other research addresses the risk of land-use conversion
70 (Strange et al. 2006), the impact of price uncertainty on different aspects of agri-environment
71 policies (Barraquand and Martinet 2011), and how to optimally allocate conservation budgets
72 over time, considering budget uncertainty (Drechsler and Wätzold 2007) and flexibility
73 (Lennox et al. 2017). Final examples are analyses on the impact of land market feedbacks on
74 reserve selection (Butsic et al. 2013), the impact of policy adjustment costs on species
75 management if ecosystems change (Boettiger et al. (2016), the cost-effective mitigation of
76 threats to biodiversity conservation (Auerbach et al. (2015), and the combination of threat
77 mitigation with different types of discounting (Armsworth 2018).

78 The overall purpose of this paper is to contribute to the application of the concepts of path
79 dependence and lock-in effects to the analysis of biodiversity conservation in a dynamic and

80 uncertain world. Our research is novel as, to our knowledge, we present the first paper that
81 applies a modelling approach to analyse path dependence and lock-in effects in biodiversity
82 conservation. More specifically, we develop a conceptual ecological-economic model to
83 identify ecological and economic parameters which might favour efficiency losses due to path
84 dependence and lock-in effects in the context of the efficient spatial allocation of conservation
85 measures.

86 For our analysis, we develop a model with two regions and two time periods, and compare
87 two settings. In a ‘myopic setting’, the conservation agency only knows before each period
88 the budget for that period and has no information about the budget in the second period. In an
89 ‘optimal setting’, the agency is informed in the beginning about the budgets available in both
90 periods. In comparison with the optimal setting, efficiency losses may occur in the myopic
91 setting due to path dependence and lock-in, such that the agency invests the budget in a region
92 where it turns out to be sub-optimal in hindsight. We analyse which characteristics of
93 economic and ecological parameters favour such efficiency losses. To demonstrate the
94 practical relevance of our findings, we present potential efficiency losses through path
95 dependence and lock-in in the hypothetical case of applying payments financed by offsets to
96 conserve the Large Blue butterfly, *Maculinea teleius*, in a region near the city of Landau in
97 Germany.

98

99 **2. Methods**

100 **2.1 The model**

101 We consider two regions that differ by their ecological benefit functions, their economic cost
102 functions and their initial habitat area. For the choice of the benefit functions we build two
103 scenarios:

104 (a) the benefit functions are concave or convex to varying degrees, such that the benefit B_i in
105 region i ($i = 1,2$) is given by:

$$106 \quad B_i = A_i^{z_i} \quad (1a)$$

107 where A_i is the habitat area in region i and z_i a region-specific constant.

108 Concave benefit functions ($z_i < 1$) may be motivated by the species-area relationship that tells
109 that the number of species in a region increases with the size of that region in a concave
110 manner (Begon et al. 1990, Table 22.1), or by the fact that the expected life time of a
111 population subject to strong environmental fluctuations increases less than linearly with
112 increasing habitat area (Lande 1993, Wissel et al. 1994). Convex benefit functions ($z_i > 1$)
113 may arise due to threshold effects or the fact that the expected life time of a population subject
114 to weak environmental fluctuations increases more than linearly with increasing habitat area
115 ((Lande 1993, Wissel et al. 1994). In the case study in section 4 we will use that (in the
116 absence of spatial environmental correlations) the viability of a metapopulation increases with
117 increasing number of habitat patches in a convex manner. Examples of concave and convex
118 benefit functions are shown in Fig. 1a.

119 (b) the benefit functions are saturating, such that the benefit is given by

$$120 \quad B_i = \frac{A_i^{z_i}}{A_i^{z_i} + k_i} \quad (1b)$$

121 where k_i and z_i are constants. In a saturating benefit function the benefit is limited to some
122 maximum value, which in the present formulation is equal to one. For $z_i > 1$ (dash-dotted and
123 long-dashed lines in Fig. 1b) the benefit increases in a convex manner with increasing habitat
124 area A_i if A_i is rather small, and in a concave manner if A_i is rather large (sigmoid shape).
125 Increasing k_i beyond the value of 2 chosen in Fig. 1b would shift the concave region towards
126 larger values of A_i . The sigmoid shape of the ecological benefit function models an ecological

127 threshold that must be crossed to reach high ecological benefits. The magnitude of habitat
128 area A_i that is needed to cross the threshold is positively related to parameter k_i , so that
129 increasing k_i shifts the threshold towards larger areas A_i .

130 For $z_i \leq 1$ (solid, dotted and short-dashed lines in Fig. 1b) the benefit B_i increases in a concave
131 manner with increasing habitat area A_i so that the marginal benefit declines with increasing A_i .
132 This case is qualitatively very similar to the case of concave benefit functions in eq. (1a)
133 discussed above.

134 Initially, each of the two regions has a habitat area of magnitude A_{0i} which may be increased
135 by amounts ΔA_i . The associated costs (depending on the policy instrument this might be
136 purchase of area, conservation payments, etc.) are modelled as

$$137 \quad C_i = c_{0i}\Delta A_i + e_i(\Delta A_i)^2, \quad (2)$$

138 so that cost C_i increases quadratically with increasing habitat area A_i . In economic terms, this
139 means that the marginal cost dC_i/dA_i increases linearly with increasing habitat area A_i , and $2e$
140 is the slope of that increase. Parameter c_{0i} is the cost of the first unit of increased habitat area.
141 Marginal costs increase because in the decision to conserve some land, the least expensive
142 land parcels are given priority, and with increasing budgets more expensive land parcels are
143 selected. Marginal costs can be shown to increase linearly if the costs of the land parcels are
144 heterogeneous and distributed according to a uniform distribution (Drechsler 2011). For
145 reasons of simplicity, we assume that the financial expenses for conservation, i.e. the budget,
146 equal costs C_i (see Wätzold and Drechsler (2014) and Drechsler (2017) for examples where
147 an efficiency analysis considers budget and costs separately).

148 The total conserved area in region i then is

$$149 \quad A_i = A_{0i} + \Delta A_i. \quad (3)$$

150 which determines the benefit B_i according to eq. (1). We assume that the total benefit in both
151 regions is

$$152 \quad B_{\text{tot}} = B_1 + B_2, \quad (4)$$

153 for an alternative assumption see Wätzold and Drechsler (2005). Based on the above settings
154 and using eq. (1a), Drechsler and Wätzold (2001) analysed the decision problem where a
155 conservation agency must allocate a budget C_{tot} among the two regions to maximise B_{tot} .

156 The control variable in that static decision problem is the budget share $q \in [0,1]$ that falls into
157 region 1, with $C_1 = qC_{\text{tot}}$ and $C_2 = (1-q)C_{\text{tot}}$ (and $C_1 + C_2 = C_{\text{tot}}$). Depending on the
158 parameters, a cost-effective share q_{opt} exists that maximizes B_{tot} for given C_{tot} .

159 Dynamics and time-dependence come into play by assuming that the budget becomes
160 available to the conservation agency in two tranches. In a first period the agency can spend a
161 budget of $C^{(1)}$ and in a second period a budget $C^{(2)}$ is available. The corresponding total
162 benefits in the two periods are calculated according to eq. (4) and denoted as $B_{\text{tot}}^{(1)}$ and $B_{\text{tot}}^{(2)}$,
163 and the total intertemporal benefit is assumed to be

$$164 \quad B = B_{\text{tot}}^{(1)} + rB_{\text{tot}}^{(2)}, \quad (5)$$

165 where r is the discount rate.

166 The task for the conservation agency is to allocate the two budgets $C_{\text{tot}}^{(1)}$ and $C_{\text{tot}}^{(2)}$ among the
167 two regions so that the intertemporal benefit B is maximised. An allocation is represented by
168 $q^{(1)}$ and $q^{(2)}$ where $C_1^{(1)} = q^{(1)}C_{\text{tot}}^{(1)}$ is the budget for region 1 in period 1, $C_2^{(1)} = (1-q^{(1)})C_{\text{tot}}^{(1)}$ is
169 the budget for region 2 in period 1, $C_1^{(2)} = q^{(2)}C_{\text{tot}}^{(2)}$ is the budget for region 1 in period 2, and
170 $C_2^{(2)} = (1-q^{(2)})C_{\text{tot}}^{(2)}$ is the budget for region 2 in period 2.

171 We consider two settings in this dynamic allocation problem:

172 (I) ‘optimal’: the conservation agency knows $C_{\text{tot}}^{(1)}$ and $C_{\text{tot}}^{(2)}$ in the beginning of the
173 first period and chooses $q^{(1)}$ and $q^{(2)}$ to maximise the intertemporal benefit B .

174 (II) ‘myopic’: in the beginning of the first period the conservation agency only knows
175 $C_{\text{tot}}^{(1)}$ and chooses $q^{(1)}$ to maximise $B_{\text{tot}}^{(1)}$. Only in the beginning of the second
176 period it learns the budget $C_{\text{tot}}^{(2)}$ for the second period and based on this
177 information chooses $q^{(2)}$ to maximise B .

178 In the myopic setting, the conservation agency allocates the budget into the two regions based
179 on the size of the currently available budget, as it has no information about the availability of
180 future budgets. This leads to path dependence in a sense that “history matters” (Liebowitz and
181 Margolis 1995): the decision in period 1 on where to allocate the conservation budget $C^{(1)}$
182 generates conservation conditions that influence the decision in period 2 on where to allocate
183 the conservation budget $C^{(2)}$. As the decisions of the first period cannot be easily reversed for
184 ecological reasons (reversal would create habitat turnover which negatively affects species:
185 Johst et al. 2011) and for economic reasons (it is not straightforward to purchase and sell
186 conservation areas, Lennox et al. 2017), the conservation investment from the first period is
187 “locked-in”.

188 Due to path dependence and the lock-in effect the intertemporal benefit in the myopic setting
189 (B_{myopic}) may be smaller than that in the optimal setting (B_{opt}). An efficiency loss occurs which
190 is measured by

$$191 \quad L = \frac{B_{\text{opt}} - B_{\text{myopic}}}{B_{\text{opt}}}. \quad (6)$$

192

193 **2.2 Model analysis**

194 To analyse the effect of the model parameters on the existence and relevance of path
195 dependencies we randomly sample the model parameter values from uniform distributions
196 (Table 1). We build 10^6 random parameter combinations and for each of them calculate the
197 efficiency loss L . We identify the set \mathcal{P} of all parameter combinations that lead to efficiency
198 losses $L \geq 0.1$ for the scenario of eq. (1a) and $L \geq 0.05$ for the scenario of eq. (1b). We are
199 interested in the statistical properties of the parameter combinations in \mathcal{P} . For this we first
200 calculate the means of the model parameters in \mathcal{P} to compare them with the means from the
201 uniform distributions of Table 1. A large difference in these means for some focal model
202 parameter indicates that efficiency losses $L \geq 0.1$ ($L \geq 0.05$) are generated by parameter values
203 that are not any more uniformly distributed but biased towards one of the two bounds of the
204 uniform range. This in turn indicates that this model parameter has a strong influence on the
205 existence of path dependence, and the sign of the difference between the two means indicates
206 whether an increase in the parameter increases or decreases the likelihood of path
207 dependence.

208 In a second step we aim at detecting interactions between model parameters and calculate
209 pairwise correlations (based on Pearson's correlation coefficient) between the parameters,
210 based on the set \mathcal{P} . To identify interactions of three or more parameters we introduce a new
211 approach which is based on the observation that if, e.g., two normalised quantities x and y
212 (with a mean of zero and a standard deviation of one) are strongly positively (negatively)
213 correlated their sum $x + y$ (difference $x - y$) has a comparatively large variation. In Appendix
214 S1 we develop a new procedure that allows analysing combinations of multiple quantities
215 with regard to positive and negative correlations and ranks them through some 'weighted'
216 sum f introduced in Appendix S1. If two model parameters a and b , e.g., have a correlated
217 effect on the likelihood of path dependence, the procedure will generate the result ' $\{a + b\}$
218 best characterises the relationship between parameters a and b ', where the plus sign represents

219 the positive correlation (a minus sign would represent a negative correlation). With three
220 model parameters, a , b and c , a typical result might be ‘ $\{a + b - c\}$ best characterises the
221 relationship between the three parameters quantities a , b and c ’, where $\{a + b - c\}$ stands for
222 ‘ a is positively correlated with b and negatively correlated with c ’. In the analysis we consider
223 interactions of up to four model parameters and identify the three strongest correlations (with
224 highest Pearson’s correlation coefficient and/or the highest value of f).

225

226 **3. Results**

227 **3.1 Concave and/or convex benefit functions**

228 We identified 17,680 parameter combinations which lead to efficiency losses L equal or
229 above 0.1. Table 2 shows the means of the parameters in this set \mathcal{P} . Some of the means differ
230 from those in Table 1: the means of z_1 and z_2 are increased, those of A_{10} and A_{20} are reduced,
231 and the mean of $C^{(1)}$ is reduced while that of $C^{(2)}$ is increased. The increased means of the
232 exponent z_1 and z_2 mean that efficiency losses are more likely to occur with strongly convex
233 benefit functions (large z). The reason is the strongly increasing marginal benefits associated
234 with strongly convex benefit functions. This implies that (i) the benefit increases fast with
235 increasing budget, it increases faster than the costs which increase only quadratically, and
236 therefore larger budgets should always be allocated into the region with the highest z_i , and that
237 (ii) substantial differences occur between the benefits of the two regions (for given habitat
238 area) even if their z values differ only slightly (Fig. 1a). These two aspects imply that extreme
239 allocations of the budget (all into one region) are most critical if in hindsight it turns out that
240 another allocation with a larger share in the other region would have been better.

241 Small initial habitat areas A_{01} and A_{02} mean that even if z_1 and z_2 differ, the initial benefits
242 $B_i(A_{0i})$ and the initial marginal benefits $dB_i(A_{i0})/dA_i$ do not yet differ strongly, so the signal for

243 allocating the budget into the region with the higher z_i is weak compared to other signals like
244 costs, so a small budget may be misguided into the region with the lower z_i .

245 To understand the result regarding the budgets $C^{(1)}$ and $C^{(2)}$, consider that in the myopic
246 setting the conservation agency decides on the first-period allocation only on the basis of $C^{(1)}$.
247 If $C^{(1)}$ is small compared to the total budget $C^{(1)} + C^{(2)}$ then due to the differing cost and
248 benefit functions there is a risk that the cost-effective allocation based on $C^{(1)}$ differs from that
249 based on $C^{(1)} + C^{(2)}$.

250 Next consider the pairwise correlations between the parameters in \mathcal{P} . Both with regard to
251 Pearson's correlation coefficients and our own procedure for detecting correlations (Appendix
252 A), the three strongest correlations are

253 (i) $z_1 + A_{02}$

254 (ii) $A_{01} - A_{02}$

255 (iii) $z_1 - A_{01}$.

256 Note that these correlations also include their symmetric counterparts, obtained by swapping
257 the region indices 1 and 2, such as, e.g., $z_2 + A_{01}$ for correlation (i), $A_{02} - A_{01}$ for correlation
258 (ii), and $z_2 - A_{02}$ for correlation (iii). Correlation (i) indicates that efficiency losses are likely if
259 the exponent z_1 and the initial habitat area A_{02} are positively correlated. A positive correlation
260 means that a comparatively large value of z_1 is related to a large value of A_{02} and a small value
261 of z_1 is related to a small value of A_{02} . To consider the first case of both parameters being
262 large, according to the benefit function eq. (1), a large A_{02} implies a comparatively large
263 initial marginal benefit in region 2, even if $z_2 < z_1$. A large value of z_1 , however, implies that
264 z_1 is likely to be larger than z_2 . Consequently, in the myopic setting the large initial marginal
265 benefit in region 2 guides the first-period budget $C^{(1)}$ into region 2 which, however, is likely
266 to have the lower z , and is more effective for larger budgets.

267 For the case of both z_1 and A_{02} being small the argument is analogous: a small A_{02} implies that
268 the initial marginal benefit in region 2 is likely to be lower than that in region 1, misguiding
269 the first-period budget $C^{(1)}$ into the region which has an exponent z_1 likely to be smaller than
270 z_2 .

271 Since the two cases of both parameters being large and both being small lead to the same
272 conclusion, we consider only one of these two cases in the interpretation of the other
273 correlations below. Analogously, if the two parameters are negatively correlated so that a
274 large value of one parameter coincides with a small value of the other (correlations (ii) and
275 (iii)), we consider only one of the two possible cases. In addition, we consider that if a
276 parameter is high for one region (e.g., large z_1) it is likely (probability above 50%) to be
277 higher than that for the other region (z_2), unless there is some significant correlation between
278 the two parameters (z_1 and z_2).

279 The (likely) efficiency loss caused by the positive correlation between z_1 and A_{02} (correlation
280 (i)), of course, occurs only if the two initial habitat areas differ (because otherwise both
281 regions would have the same initial marginal benefit), which is indicated by correlation (ii)
282 telling that efficiency losses occur especially if A_{01} and A_{02} are negatively correlated, i.e. when
283 one of them is large and the other one is small.

284 The negative correlation (iii) between z_1 and A_{01} can be explained in the same way as
285 correlation (i). For instance, a large value of A_{01} implies a high initial marginal benefit in
286 region 1 and in the myopic setting the budget $C^{(1)}$ is likely to be allocated into region 1. This
287 region, however has a small z_1 which calls for allocation of the budget into region 2 (with the
288 probably higher exponent $z_2 > z_1$) in the optimal setting.

289 The three strongest triple correlations are (again not listing their symmetric counterparts):

290 (iv) $z_1 - A_{01} + A_{02}$

291 (v) $z_1 - z_2 - A_{01}$

292 (vi) $z_1 - z_2 + A_{02}$.

293 They represent combinations or ‘amplifications’ of the three pairwise correlations above and
294 can be explained in the same way. Correlation (iv), for instance, amplifies correlation (ii)
295 above, so that efficiency losses occur especially if the initial habitat areas are negatively
296 correlated, and if in addition the exponent z_1 in region 1 is negatively correlated with A_{01}
297 (correlation (iii)).

298 The three strongest quadruple correlations are:

299 (vii) $z_1 - z_2 - A_{01} + A_{02}$

300 (viii) $z_1 - c_{02} - A_{01} + A_{02}$

301 (ix) $z_1 - e_1 - A_{01} + A_{02}$.

302 Correlation (vii) is again a combination or amplification of the previous correlations.
303 Correlations (viii) and (ix), in contrast, add some new information. Regarding correlation
304 (viii), in the myopic setting the component $z_1 - A_{01} + A_{02}$ is likely to misguide the budget $C^{(1)}$
305 into region 2 with the higher initial habitat area and marginal benefit. This is amplified by a
306 small initial marginal cost c_{02} (c_{02} is positively correlated with A_{02} in correlation (viii)). In an
307 analogous manner we can explain correlation (ix): in the myopic setting a large slope of the
308 marginal cost e_1 misguides the budget $C^{(1)}$ away from the more costly region 1 although it is
309 likely to have the higher exponent z_1 and would receive the entire budget $C^{(1)} + C^{(2)}$ in the
310 optimal setting.

311

312 **3.2 Saturating benefit functions**

313 As Table 2 shows, some of the means in set \mathcal{P} differ from those in Table 1. The main
314 differences are that the means of the initial habitat areas, A_{01} and A_{02} , and the budgets, $C^{(1)}$ and
315 $C^{(2)}$, are smaller, with the mean of the first-period budget $C^{(1)}$ being much smaller than that of
316 the second-period budget $C^{(2)}$. Although the means of the exponents z_1 and z_2 are only slightly
317 higher than the means in Table 1, they represent sigmoid benefit functions in which the
318 ecological benefit first increases on a convex manner and later in a concave manner (Fig. 1b).
319 Together with this observation, the relatively small means of A_{01} , A_{02} , $C^{(1)}$ and $C^{(2)}$ indicate
320 that the problem of efficiency losses due to path dependence and lock-in effects occurs
321 especially when the amounts of conserved areas are such that the convex part of the
322 ecological benefit function governs the ecological benefit. By this, similar arguments apply as
323 with concave and/or convex benefit functions.

324 This is confirmed by the observation that the three strongest pairwise correlations obtained
325 with saturating benefit functions between the parameters in \mathcal{P} are identical to the correlations
326 (i) – (iii) obtained with concave and/or convex benefit functions; and the strongest triple and
327 quadruple correlations are very similar to correlations (iv) – (ix) above.

328

329 **4. Case study**

330 To illustrate the practical relevance of path dependence and lock-in, we consider the
331 conservation of the endangered Large Blue butterfly, *Maculinea teleius*, in a landscape near
332 the city of Landau in Germany (Drechsler et al. 2007). If the meadows in the landscape (Fig.
333 2) are managed in a profit-maximising manner, they are mown every year at the end of May
334 and a second time in mid-July. The second cut thus falls into the eclosion period of the
335 butterfly, reducing the species' reproductive success. As a conservation measure, we consider
336 an alternative mowing regime: mowing every second year once at the end of August. This

337 mowing regime maximises butterfly survival in the study region for a given budget, without
338 harming breeding birds (Drechsler et al., 2010). As shown by the authors, the survival of the
339 butterfly is sensitive to the spatial allocation of meadows on which this alternative, butterfly-
340 friendly mowing regime is applied. In particular, butterfly survival increases with increasing
341 spatial aggregation of the butterfly-friendly meadows.

342 We assume that the butterfly-friendly mowing regime is incentivised through payments from
343 offsets, which are available in Germany (OECD 2016). The offsets compensate for long-term
344 negative impacts on the environment. Therefore, contracts where farmers commit themselves
345 to manage their land in a certain biodiversity-enhancing manner in return to payments, have to
346 be long-term (typically 30 years), too (Treffkorn et al. 2007, OECD 2016). We extend the
347 analysis of Drechsler et al. (2007) with the butterfly-friendly mowing regime of Drechsler et
348 al. (2010) to a dynamic management problem by assuming two periods, each consisting of 15
349 years, where in the first period a budget is available that allows total payments of €10,000 per
350 annum and in the second period of €20,000 per annum. The budget increase between the two
351 periods mimics the setting of the general model analysis that in the second period more land
352 can be conserved than in the first. Assuming profit-maximising behaviour, landowners with
353 costs below the payment will accept the payment and mow in the butterfly-friendly manner
354 while landowners with higher costs manage their land in the profit-maximising manner.

355 We further assume that in the west of the study region (left to the vertical dotted line in Fig. 2,
356 termed the western subregion), marginal conservation costs are lower than in the eastern
357 subregion (right to the vertical dotted line in Fig. 2). This is motivated by the assumption of
358 farm houses being located in the more rural eastern subregion, implying that the reduced
359 mowing frequency of the butterfly-friendly mowing regime reduces transport costs from the
360 *distant* meadows in the western subregion to the farm houses (relative to the transport costs
361 associated with the profit-maximising mowing regime which involves more frequent

362 mowing). We add these spatially differentiated transport costs to the conservation costs of
363 Drechsler et al. (2007) by multiplying those costs in the eastern subregion by a factor $b = 2$.

364 Second, we assume that transport costs are lower if the managed meadows are close to each
365 other. This is relevant especially in the eastern subregion where the meadows are closer to the
366 farm houses, because here a dispersion of the meadows adds relatively more to the transport
367 costs than in the western subregion in which all meadows are associated with rather high
368 transport costs. To model this circumstance in a simple and intuitive manner, we assume that
369 the costs (per hectare) around the point marked by the open circle in Fig. 2 are reduced by

$$370 \quad \Delta c = -h \exp(-\alpha r) \quad (7)$$

371 with $h = \text{€}400$ and $\alpha = (1.25 \text{ km})^{-1}$. At the marked point the costs reduction therefore is $\Delta c =$
372 $\text{€}400$ and which declines with increasing distance so that one km from the point it equals
373 about $\Delta c = \text{€}180$.

374 The second assumption, together with the fact that the payment scheme induces conservation
375 of the least costly meadows, implies that in the eastern subregion butterfly-friendly meadows
376 will be spatially aggregated, while in the western subregion they will not. Metapopulation
377 theory (Hanski 1999) states that (at least in the absence of correlated environmental
378 stochasticity) the viability of a metapopulation increases with increasing number of habitat
379 patches in a convex manner (e.g., Frank and Wissel 2002), and the strength of this convexity
380 is positively related to the spatial connectivity of the habitat patches (Frank and Wissel 2002).
381 So the viability of the butterfly population in the study region will increase in a convex
382 manner with increasing number of butterfly-friendly meadows, and the convexity is stronger
383 if butterfly-friendly meadows are added in the eastern subregion than in the western
384 subregion.

385 Together with our first assumption that marginal conservation costs are higher in the eastern
386 subregion than in the western subregion, we are confronted with a typical situation identified
387 in the general model analysis that favours path dependence and lock-in: the ecological benefit
388 functions are convex, and the more convex benefit function is associated with higher marginal
389 conservation costs.

390 Lock-in arises in the present management problem because the contracts between
391 conservation agency and farmer have a duration of 30 years implying that a meadow
392 conserved in year 1 of the analysis will stay conserved for the next 30 years. The problem of
393 path dependence occurs because in the first 15-year period a rather small conservation budget
394 is available which may favour a different allocation of butterfly-friendly meadows than the
395 larger budget available in the second 15-year period. This change in the cost-effective
396 allocation would call for a reallocation of butterfly-friendly meadows, which however is
397 impossible due to the lock-in.

398 From the results of the general model analysis we expect that under the myopic setting the
399 conservation agency will, given its small budget in the first period and its aim for cost-
400 effectiveness, allocate the butterfly-friendly meadows in the less costly western subregion –
401 which is achieved by offering conservation contracts for *all* meadows in the study region. In
402 contrast, under the optimal setting where the budget increase to the second period is known it
403 is cost-effective to offer the contracts only for meadows in the *eastern* subregion, because at
404 larger budgets it is more cost-effective to allocate, despite the higher costs, conservation
405 efforts into the region with the more convex benefit function – which in the present case is the
406 eastern subregion.

407 Figure 3 confirms these expectations. In the first period (lines without symbols) the
408 quasiextinction risk of the butterfly is smaller if conservation contracts are offered for all
409 meadows in the study region (dotted line) than if they are offered only for meadows in the

410 eastern subregion (solid line). So in the myopic setting the conservation agency would offer
411 the contracts for all meadows. In the second period (lines with symbols), in contrast, the
412 quasiextinction risk is lower if the contracts had been offered right from year 1 only for
413 *eastern* meadows (solid line) than if they were offered for *all* meadows over the entire 30
414 years (dotted line) or if they had been offered for all meadows in the first period and were
415 offered only for the eastern meadows in the second period (dashed line). Altogether, if only
416 the first period is considered it is more cost-effective to offer the contracts for all meadows
417 while if the longer future is considered it is more cost-effective to offer them only for
418 meadows in the eastern subregion.

419 As the case study only served to illustrate the potential relevance of our general analysis for
420 real-world conservation, a systematic analysis of the driving factors of the results is beyond
421 the scope of this paper. However, we analysed two alternative scenarios without (i) reduced
422 differences in the strengths of convexity (by largely eliminating the spatial clustering of
423 butterfly-friendly meadows in the eastern subregion and setting $\alpha = (0.125 \text{ km})^{-1}$) and (ii)
424 reduced differences in the marginal conservation costs between the two subregions (by
425 reducing b to 1.5), and observed no path dependence: offering the contracts for *all* meadows
426 always minimised the quasiextinction risk. This indicates that the path dependence observed
427 in the case study indeed results from the described positive correlation between marginal
428 conservation costs and strength of convexity in the ecological benefit function.

429

430 **5. Summary of results and discussion**

431 Efficiency losses due to path dependence and lock-in effects are likely if there are signals that
432 misguide the first-period budget into a region that is suboptimal in terms of cost-effectiveness
433 if both time periods were considered right from the beginning. These wrong signals are

434 mainly sent from the marginal costs and benefits. Large initial costs and/or small initial
435 marginal ecological benefits in one region are likely to guide the first-period budget into the
436 other region. This other region, however, may have a less strongly increasing ecological
437 benefit function if both time periods and both budgets were considered.

438 In our model, this occurs especially if

- 439 (i) the ecological benefits functions are strongly convex, so that the benefit increases
440 at an increasing rate,
- 441 (ii) level and slope of marginal costs are small in the region with the less convex
442 benefit function, so that the first-period budget is misguided into the region which
443 in the long run has the lower ecological benefit,
- 444 (iii) the initial habitat area, and thus the initial marginal benefit is small in the region
445 with the more convex benefit function, so that the first-period budget is misguided
446 into the other region which in the long run has the lower ecological benefit.

447 The conservation relevance of the findings is demonstrated by a case study where offset
448 payments are applied to butterfly conservation near the city of Landau, Germany.

449 Naturally, the problem of path dependence occurs if the budget for the first period is
450 substantially smaller than the total budget available for both periods. If it was almost as large
451 as the total budget the allocation signal for the first-period allocation would likely to be the
452 same as that for the allocation of the total budget. On the other hand, it is plausible (not
453 analysed systematically in this paper) that an extremely small first-period budget would not
454 lead to large efficiency losses, because even if it was allocated into the wrong region, the
455 associated 'waste of money' would be small.

456 The insights from our model can be generalised to make them fruitful to a broader
457 conservation context. The model results indicate a principle structure where in a situation with

458 several conservation projects and uncertainty over future budgets, path dependence and lock-
459 in effects with efficiency losses are likely to occur: This is the case if marginal net benefits
460 (benefit minus costs) of some projects in the first period are high but in later period(s) low and
461 for other projects the opposite applies. Myopic concerns of cost-effectiveness (under
462 uncertainty) then suggest allocating resources in the first type of projects whereas with
463 hindsight and over a long time the opposite allocation might have been the more cost-
464 effective option. Our case study suggests that such a structure might not be uncommon in
465 conservation decisions, calling for more research on path dependence and lock-in effects in
466 biodiversity conservation, the efficiency losses that arise and policy responses to avoid them.

467 Although these conclusions are derived from an analysis with two periods, we believe that in
468 their general sense they are valid also in conservation management problems with more than
469 two periods. Nevertheless, extending the analysis two more than two periods would be an
470 interesting matter of future research.

471 A straightforward policy recommendation from our analysis is that uncertainty over future
472 budgets should be minimized to the extent possible to avoid efficiency losses due to path
473 dependence and lock-in effects. This conclusion – based on a conceptual model – is in line
474 with calls from practitioners in several European countries who consider uncertainty over
475 future budgets a main impediment for cost-effective conservation activities (Wätzold et al.
476 2010). This indicates a high relevance of the issue of budget uncertainty and that better
477 conservation outcomes can be achieved if information about future conservation budgets is
478 available at an early stage.

479 In our opinion, there is substantial potential for further research to understand under what
480 ecological and economic conditions path dependence and lock-in effects in biodiversity
481 conservation occur and how conservation policy responses should look like. In our case,
482 budget uncertainty leads to path dependence and lock-in effects. However, other factors may

483 also favour or hinder their occurrence. A possible factor is the flexibility of policy instruments
484 to respond to changing ecological and societal circumstances. For example, some people
485 argue that conservation banking may be a flexible policy instrument able to respond to change
486 (Johst et al. 2011, Wende et al. 2018) whereas other policy instruments such as conservation
487 easements are criticised for lacking flexibility (Rissman et al. 2013). In how far inflexibility
488 of policy instruments contributes to path dependence and lock-in effects is a matter of further
489 research and we hope this paper can stimulate this and related debates. These debates seem
490 important from a conservation point of view, as our analysis suggests that if path dependence
491 and lock-in effects are not considered, efficiency losses may occur resulting in a waste of
492 scarce conservation resources (cp. Ferraro and Pattanyak 2006, Cong and Brady 2012).

493

494 **References**

495 Armsworth PR. 2018. Time discounting and protected-area priorities. *Conservation Biology*
496 **32**:1063–1073.

497 Auerbach NA, Wilson KA, Tulloch AIT, Rhodes JR, Hanson JO, Possingham HP. 2015.
498 Effects of threat management interactions on conservation priorities. *Conservation Biology*
499 **29**:1626–1635.

500 Barraquand F, Martinet V. 2011. Biological conservation in dynamic agricultural landscapes:
501 effectiveness of public policies and trade-offs with agricultural production. *Ecological*
502 *Economics* **70**: 910–920.

503 Barnett JL, Evans S, Gross C, Kiem AS, Kingsford RT, Palutikof JP, Pickering CM,
504 Smithers SG. 2015. From barriers to limits to climate change adaptation: path dependency and
505 the speed of change. *Ecology and Society* **20**:5.

506 Begon M, Townsend CR, Harper JL. 1990. Ecology: From Individuals to Ecosystems.
507 Blackwell, 2nd ed.

508 Bidaud C, Méral P, Andriamahefazafy F, Serpantié G, Cahen-Fourot L, Toillier A. 2013.
509 Institutional and historical analysis of payments for ecosystem services in Madagascar.
510 Governing the provision of ecosystem services. Pages 207–233, Springer, Dordrecht.

511 Boettiger C, Bode M, Sanchirico JN, LaRiviere J, Hastings A, Armsworth PR. 2016. Optimal
512 management of a stochastically varying population when policy adjustment is costly.
513 Ecological Applications **26**:808–817.

514 Butchart SH, Walpole M, Collen B, Van Strien A, Scharlemann JP, Almond RE., ...
515 Carpenter KE. 2010. Global biodiversity: indicators of recent declines. Science **328**:1164–
516 1168.

517 Butsic V, Lewis DJ, Radeloff VC. 2013. Reserve selection with land market feedbacks.
518 Journal of Environmental Management **114**:276–284.

519 Cong R-G, Brady M. 2012. How to design a targeted agricultural subsidy system: efficiency
520 or equity? PLoS One 72012: e41225.

521 Costello C, Polasky S. 2004. Dynamic reserve site selection. Resource and Energy Economics
522 **26**:157–174.

523 Dallimer M, Tinch D, Acs S, Hanley N, Southall HR, Gaston KJ, Armsworth PR. 2009. 100
524 years of change: examining agricultural trends, habitat change and stakeholder perceptions
525 through the 20th century. Journal of Applied Ecology **46**:334–343.

526 David PA. 1985. Clio and the Economics of QWERTY. The American Economic Review
527 **75**:332–337.

528 Drechsler M, Wätzold, F. 2001. The importance of economic costs in the development of
529 guidelines for spatial conservation management. *Biological Conservation* **11**:51–59.

530 Drechsler M, Wätzold F. 2007. The optimal dynamic allocation of conservation funds under
531 financial uncertainty. *Ecological Economics* **61**:255–266.

532 Drechsler M. 2011. Trade-offs in the design of cost-effective habitat networks when
533 conservation costs are variable in space and time. *Biological Conservation* **144**:479–489.

534 Drechsler M. 2017. Generating spatially optimized habitat in a trade-off between social
535 optimality and budget efficiency. *Conservation Biology* **31**:221–225

536 Ferraro PJ, Pattanayak SK. 2006. Money for nothing? A call for empirical evaluation of
537 biodiversity conservation investments. *PLoS Biology* **4**:e105.

538 Haila Y, Henle K. 2014. Uncertainty in biodiversity science, policy and management: a
539 conceptual overview. *Nature Conservation* **8**:27.

540 Johst K, Drechsler M, van Teeffelen A, Hartig F, Vos CC, Wissel S, Wätzold F, Opdam P.
541 2011. Biodiversity conservation in dynamic landscapes: trade-offs between number,
542 connectivity and turnover of habitat patches. *Journal of Applied Ecology* **48**:1227–1235.

543 Lande R. 1993. Risks of population extinction from demographic and environmental
544 stochasticity and random catastrophes. *The American Naturalist* **142**:911–927.

545 Lennox GD, Fargione J, Spector S, Williams G, Armsworth PR. 2017. The value of flexibility
546 in conservation financing. *Conservation Biology* **31**:666–674.

547 Liebowitz SJ, Margolis, SE. 1995. Path dependence, lock-in, and history. *Journal of Law,*
548 *Economics, & Organization* 205–226.

549 Meir E, Andelman S, Possingham HP. 2004. Does conservation planning matter in a dynamic
550 and uncertain world? *Ecology Letters* **7**:615–622.

551 Morales-Hidalgo D, Oswalt SN, Somanathan E. 2015. Status and trends in global primary
552 forest, protected areas, and areas designated for conservation of biodiversity from the Global
553 Forest Resources Assessment 2015. *Forest Ecology and Management* **352**:68–77.

554 North DC. 1991. Institutions. *Journal of Economic Perspectives* **5**:97–112.

555 Pressey RL, Cabeza M, Watts ME, Cowling RM, Wilson KA. 2007. Conservation planning in
556 a changing world. *Trends in Ecology & Evolution* **22**:583–592.

557 Rissman A, Bihari M, Hamilton C, Locke C, Lowenstein D, Motew M, Smail R. 2013. Land
558 management restrictions and options for change in perpetual conservation easements.
559 *Environmental Management*, **52**:277–288.

560 Ruttan VW. 1997. Induced innovation, evolutionary theory and path dependence: sources of
561 technical change. *The Economic Journal* **107**:1520–1529.

562 Schöttker O, Wätzold F. 2018. Buy or lease land? Cost-effective conservation of an
563 oligotrophic lake in a Natura 2000 area. *Biodiversity and Conservation* **27**:1327–1345.

564 Strange N, Thorsen BJ, Bladt J. 2006. Optimal reserve selection in a dynamic world.
565 *Biological Conservation* **131**:33–41.

566 Sutherland LA, Burton RJ, Ingram J, Blackstock K, Slee B, Gotts N. 2012. Triggering
567 change: towards a conceptualisation of major change processes in farm decision-making.
568 *Journal of Environmental Management* **104**:142–151.

569 Sydow J, Schreyögg G, Koch J. 2009. Organizational path dependence: Opening the black
570 box. *Academy of Management Review* **34**:689–709.

571 Treffkorn A, Jessel B, Szaramowicz M. 2007. Kompensationsmaßnahmen und
572 Landwirtschaft. *Naturschutz und Landschaftsplanung* **39**:2.

573 Unruh GC, Carrillo-Hermosilla J. 2006. Globalizing carbon lock-in. *Energy Policy* **34**:1185–
574 1197.

575 Van Teeffelen AJ, Vos CC, Opdam P. 2012. Species in a dynamic world: consequences of
576 habitat network dynamics on conservation planning. *Biological Conservation* **153**:239–253.

577 Wätzold F, Drechsler M. 2005. Spatially uniform versus spatially heterogeneous
578 compensation payments for biodiversity-enhancing land-use measures. *Environmental and*
579 *Resource Economics* **31**:73–93.

580 Wätzold F, Drechsler M. 2014. Agglomeration payment, agglomeration bonus or
581 homogeneous payment? *Resource and Energy Economics* **37**:85–101.

582 Wätzold F, Mewes M, van Apeldoorn R, Varjopuro R, Chmielewski TJ, Veeneklaas F,
583 Kosola ML. 2010. Cost-effectiveness of managing Natura 2000 sites: an exploratory study for
584 Finland, Germany, the Netherlands and Poland. *Biodiversity and Conservation* **19**:2053–2069.

585 Wende W, Tucker GM, Quétier F, Rayment M, Darbi M. (Eds.). 2018. *Biodiversity Offsets:*
586 *European Perspectives on No Net Loss of Biodiversity and Ecosystem Services*. Springer.

587 Wissel C, Stephan T, Zschke S-H. 1994. Modelling small populations. Pages 67–103 in
588 Remmert H, editor. *Minimum Viable Populations*. Springer, Berlin/London/New York.

590 Table 1: Ranges for the model parameters.

Parameter	Meaning	Minimum	Maximum	Mean
z_i	Exponent benefit function (eq. 1a)	0	5	2.5
k_i	Threshold in sigmoid benefit (eq. 1b)	0	10	5
c_{0i}	Offset marginal cost function (eq. 2)	0	1	0.5
e_i	Slope marginal cost function (eq. 2)	0	5	2.5
A_{0i}	Initial conserved area region i (eq. 3)	0	10	5
$C_{\text{tot}}^{(1)}$	Budget period 1	0	10	5
$C_{\text{tot}}^{(2)}$	Budget period 2	0	10	5
r	Discount rate for benefit (eq. 5)	0	0.1	0.05

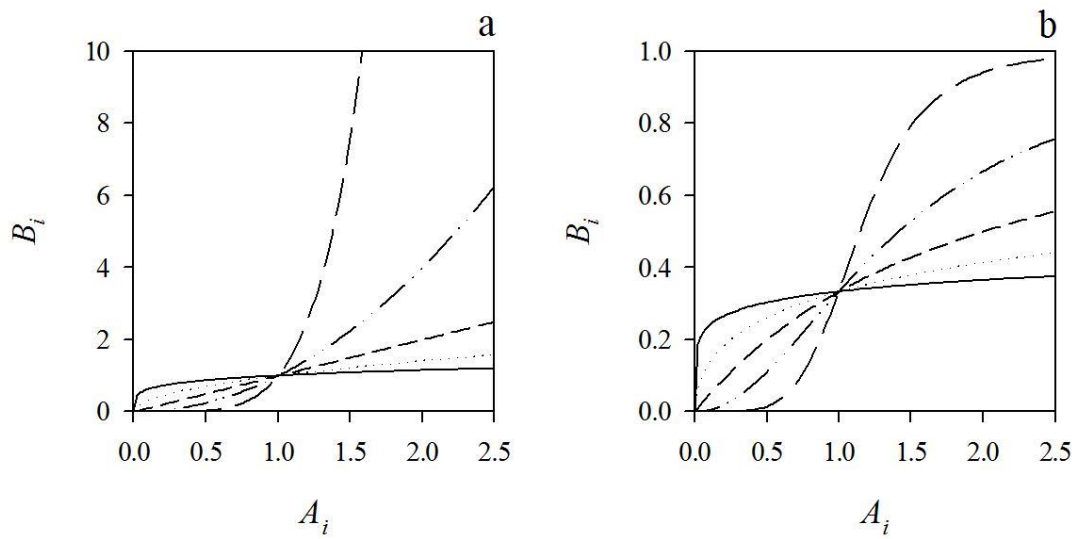
592 Table 2: Means of the parameter values in the set \mathcal{P} of parameter combinations that lead to
593 efficiency loss $L \geq 0.1$ (concave and/or convex benefit functions, scenario a) and $L \geq 0.05$
594 (saturating benefit functions, scenario b), respectively. In parentheses the comparison with the
595 means from the uniform distributions of Table 1.

Parameter	Mean (concave/convex)	Mean (saturating)
Benefit exponent z_1	3.38 (> 2.5)	2.77 (> 2.5)
Benefit exponent z_2	3.39 (> 2.5)	3.04 (> 2.5)
Threshold k_1	-	5.80 (≈ 5)
Threshold k_2	-	5.92 (≈ 5)
Initial marginal cost c_{01}	0.51 (≈ 0.5)	0.52 (≈ 0.5)
Initial marginal cost c_{02}	0.51 (≈ 0.5)	0.53 (≈ 0.5)
Slope marginal cost e_1	2.43 (≈ 2.5)	2.95 (> 2.5)
Slope marginal cost e_2	2.42 (≈ 2.5)	2.74 (≈ 2.5)
Initial habitat area A_{01}	3.72 (< 5)	1.84 (< 5)
Initial habitat area A_{02}	3.68 (< 5)	1.47 (< 5)
Budget period 1 $C^{(1)}$	3.25 (< 5)	0.96 (< 5)
Budget period 2 $C^{(2)}$	6.56 (> 5)	1.97 (< 5)
Discount rate r	0.05 ($= 0.05$)	0.05 ($= 0.05$)

596

597 **Figures**

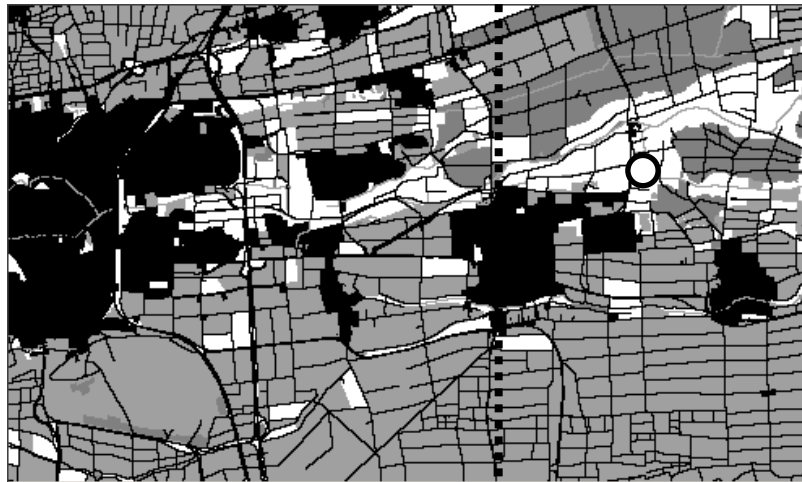
598 Figure 1: Concave and convex benefit functions (panel a) for different values of z_i (solid line:
599 $z_i = 0.2$, dotted line: $z_i = 0.5$, short-dashed line: $z_i = 1$, dash-dotted line: $z_i = 2$, long-dashed
600 line: $z_i = 5$). Saturating benefit functions (panel b) for $k_i = 2$ and different values of z_i (values
601 as in panel a).



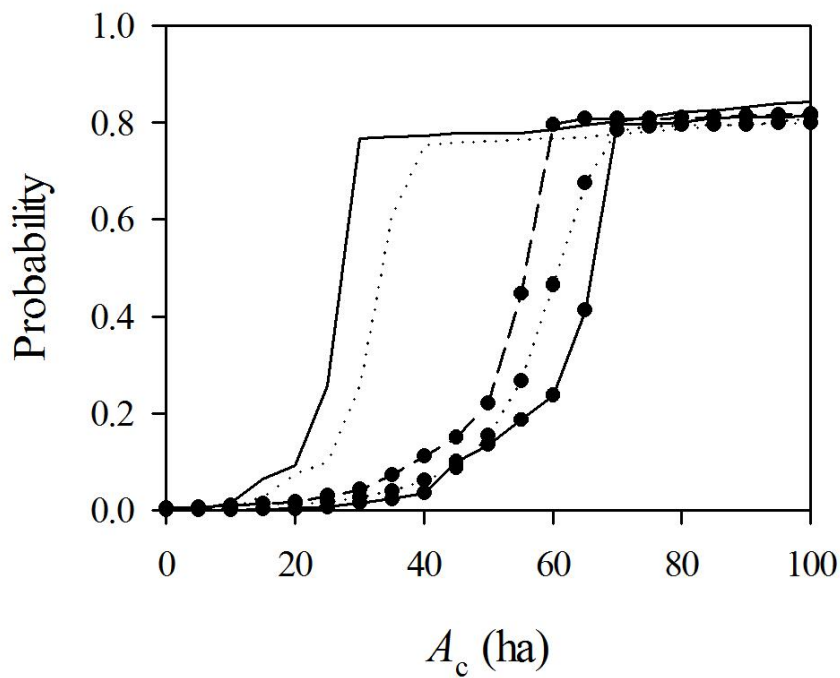
602

603 Figure 2: Model landscape (black: settlements, dark grey: forest, light grey: open land, white:
604 meadow). Source: Drechsler et al. (2007). The dotted line separates the eastern subregion
605 defined in section 4 from the western subregion, and the open circle marks the location at
606 which the cost reduction introduced by eq. (7) is maximal.

607



608 Figure 3: Quasiextinctions risk: probability of the area occupied by the butterfly falling below
609 the threshold A_c within a 15-year time period as a function of Area. Lines without symbols:
610 first period (years 1 – 15); lines with symbols: second period (years 16 – 30). Solid lines:
611 optimal setting; dotted lines: myopic setting with payment offered to all farmers in both
612 periods; dashed line: myopic setting with payment offered to all farmers in the first period and
613 only to the farmers in the eastern part of the region in the second period.



614

615

616 **Appendix S1: Development of a procedure to detect interactions among multiple**
617 **quantities**

618 The development of the procedure starts with the observation that the variation in the sum of
619 two normalised quantities a and b (with zero means and standard deviations of one)
620 monotonically increases with increasing Pearson's correlation coefficient between the two
621 quantities. To understand the reason, assume a and b to be strongly positively correlated
622 (Pearson's correlation coefficient close to 1). This means that large a are associated with large
623 b and small a are associated with small b . Consequently, the sum $a + b$ will have a rather high
624 standard deviation (close to 2 given a and b are normalised as described). In contrast, if a and
625 b were uncorrelated (with zero Pearson's correlation coefficient) a large value of a could well
626 occur with a medium or small value of b and the standard deviation of $a + b$ would be lower.
627 In the case of negatively correlated a and b (Pearson's correlation coefficient of -1) a large
628 value of a would be associated with a small value of b and a small value of a with a large
629 value of b , implying that the standard deviation of $a + b$ would be minimal (close to 0 given
630 the normalization described above). Figure A1 shows the relationship between the standard
631 deviation of the sum $a + b$ and Pearson's correlation coefficient between a and b .

632 In an analogous manner one can show that the standard deviation of the difference $a - b$
633 increases with decreasing Pearson's correlation coefficient between a and b and, in particular,
634 has a minimum value of 0 if a and b are perfectly positively correlated and a maximum value
635 of 2 if a and b are perfectly negatively correlated.

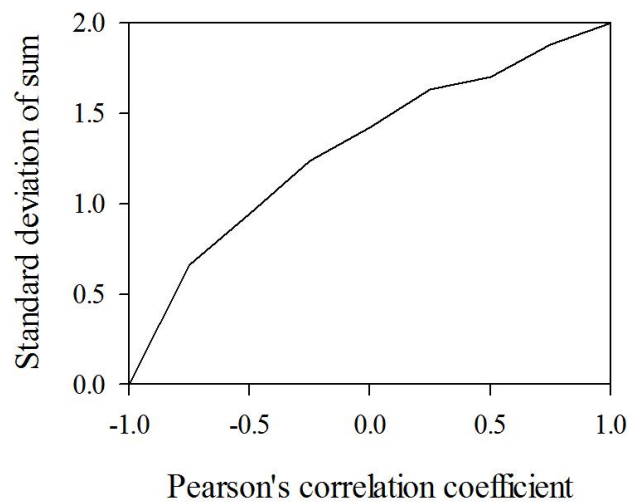
636 To consider interactions between three or more quantities, $a_1 \dots a_N$, we first normalise the a_i ,
637 so each of them has zero mean and a standard deviation of one, and build all possible
638 functions

639 $f(a_1, \dots, a_N; w_1, \dots, w_N) = w_1 a_1 + w_2 a_2 + \dots + w_N a_N$ (A1)

640 where each w_i can take values of -1 , 0 or $+1$. By this, each quantity a_i is combined with the
641 other quantities a_j ($j \neq i$) either in an additive manner ($w_i = 1$), a subtractive manner ($w_i = -1$)
642 or not at all ($w_i = 0$), and by systematically varying all w_i within their ranges all combinations
643 of positive and negative correlations between the quantities $a_1 \dots a_N$ are considered. We restrict
644 our analysis to a maximum of four interacting model parameters, i.e., $\sum_i |w_i| \leq 4$. We rank the
645 combinations $\{w_i\}$ with regard to the magnitude of function f and identify the combinations
646 with the highest values of f .

647

648 Figure A1: Standard deviation of the sum $a + b$ of two quantities a and b (each with zero
649 mean and standard deviations of one) versus Pearson's correlation coefficient between a and
650 b . The statistics are calculated on the basis of 1000 samples of a and b .



651

652